# Architectures of Exoplanetary Systems: A Forward Model for Planets around Kepler's FGK Stars with Clustered Periods and Sizes <br> PennState <br> Eberly College of Science <br> PENNSTATE <br> Center for Exoplanets and Habitable Worlds <br> Matthias Y. He ${ }^{1}$, Eric B. Ford ${ }^{1}$, Darin Ragozzine ${ }^{2}$ <br> 1. Department of Astronomy \& Astrophysics, Center for Exoplanets and Habitable Worlds, The Pennsylvania State University 2. Department of Physics \& Astronomy, Brigham Young University 

## Introduction

Thousands of exoplanet candidates have been discovered to date, thanks to NASA's Kepler mission. This explosion in the number of known exoplanet systems has enabled population studies, allowing us to probe system architectures and to develop theories for planet formation.

We present several statistical models in the context of a forward modeling framework for the Kepler mission, which can generate underlying populations of exoplanets that reproduce the observed data and allows us to infer properties of planetary systems in general.

## We forward model the Kepler mission

$f(P, R) \quad$| Step 1: Define a statistical model for the intrinsic distribution of |
| :--- |
| exoplanetary systems. |

Step 2: Generate an underlying population of exoplanetary systems (physical catalog) from a given model.


Step 3: Generate an observed population of exoplanetary systems (observed catalog) from the physical catalog.

Step 4: Compare the simulated observed catalog with the Kepler data.

Step 5: Optimize a distance function to find the best-fit model parameters.

Step 6: Explore the posterior distribution of model parameters using a Gaussian Process (GP) emulator.

| Models for intrinsic planetary systems |  |  |
| :--- | :--- | :--- |
| $\begin{array}{l}\text { Non-clustered: } \\ \text { Planets are drawn } \\ \text { independently with } \\ \text { power-law for orbital } \\ \text { periods and broken } \\ \text { power-law for radii. }\end{array}$ | $\begin{array}{l}\text { Clustered Periods: } \\ \text { Planets are drawn from } \\ \text { clusters, where their } \\ \text { periods are conditional } \\ \text { on each cluster's period } \\ \text { scale. }\end{array}$ | $\begin{array}{l}\text { Clustered Periods and } \\ \text { Sizes: }\end{array}$ |
| Planets are drawn from |  |  |
| lusters, where their periods |  |  |
| and radii are conditional on |  |  |
| each cluster's period and |  |  |
| radius scale. |  |  |$\}$



[^0] labeled), with the Kepler data plotted in gray (we include all planet candidates from DR25 with orbital periods between 3-300 days and measured radii between $0.5-10 R_{\oplus}$ ).
The Clustered Periods and Sizes model best fits the Kepler data.


Figure 2: Simulated physical catalogs for each of our three models (colored as labeled): distributions of the true number of planets per system, orbital periods, period ratios, planet radii, and planet radii ratios. The right side shows a sample of 100 systems with $8+$ planets from our Clustered Periods and Sizes model, with colors denoting various clusters of planets.


## Summary

We present a pipeline for generating populations of intrinsic exoplanetary systems and simulating observed catalogs of transit detections under the conditions of a Kepler-like mission. Using this program, we developed and fit three physically motivated, statistical models to the Kepler data.

A simple model involving independently drawn periods and sizes is inadequate for describing the Kepler population, especially that of the multi-transiting systems. We provide a forward model for generating planetary systems with planets clustered in both periods and sizes that reproduces the key features of the Kepler exoplanet population.

## References and Acknowledgements

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[^0]:    Figure 1: Simulated observed catalogs for each of our three models (colored histograms as

